

Measuring Milliohms and PicoHenrys in Power Distribution Networks

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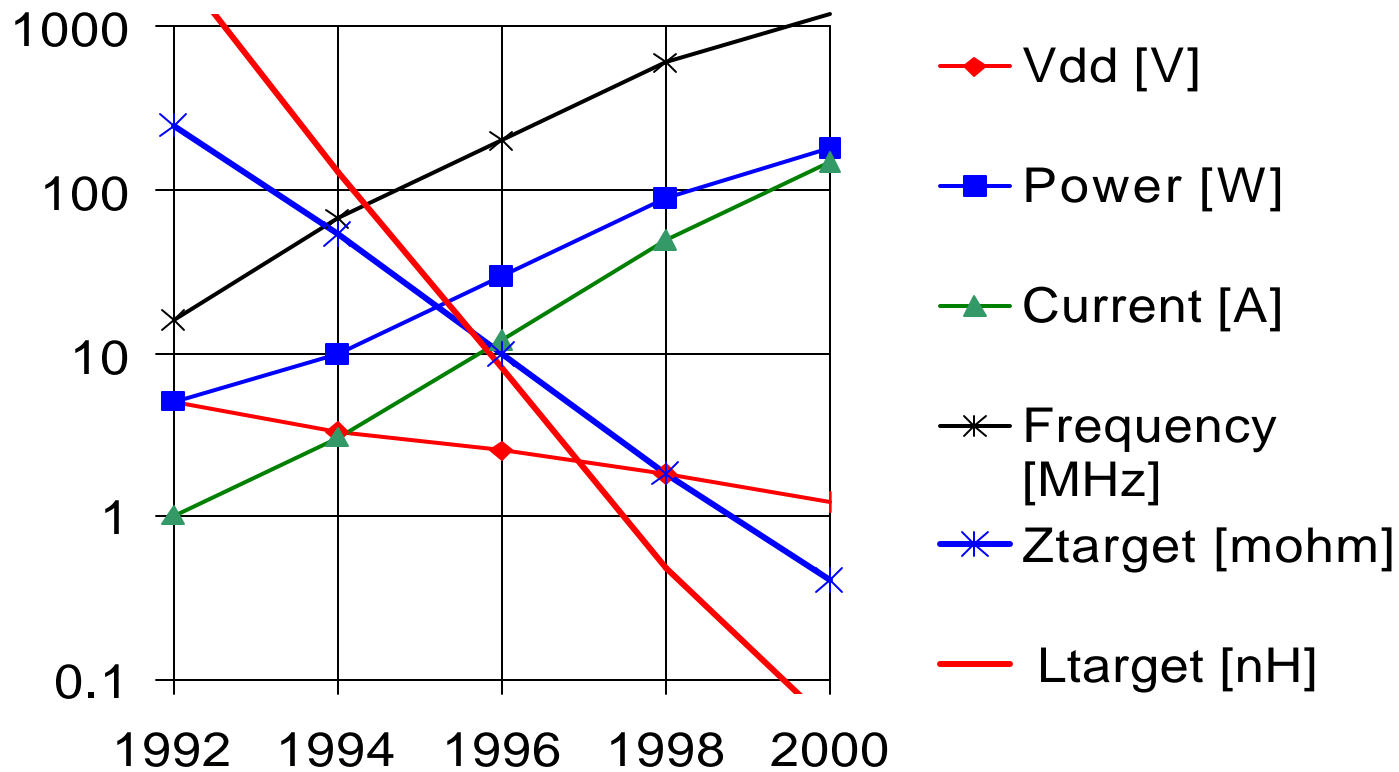
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Outline

- Introduction
- Two-port VNA impedance measurements
- Low-frequency limitations
- Enhancement with transformer or amplifier
- High-frequency limitations
- Enhancement with ferrite-covered cable
- Measured power-distribution networks
- Resources
- References

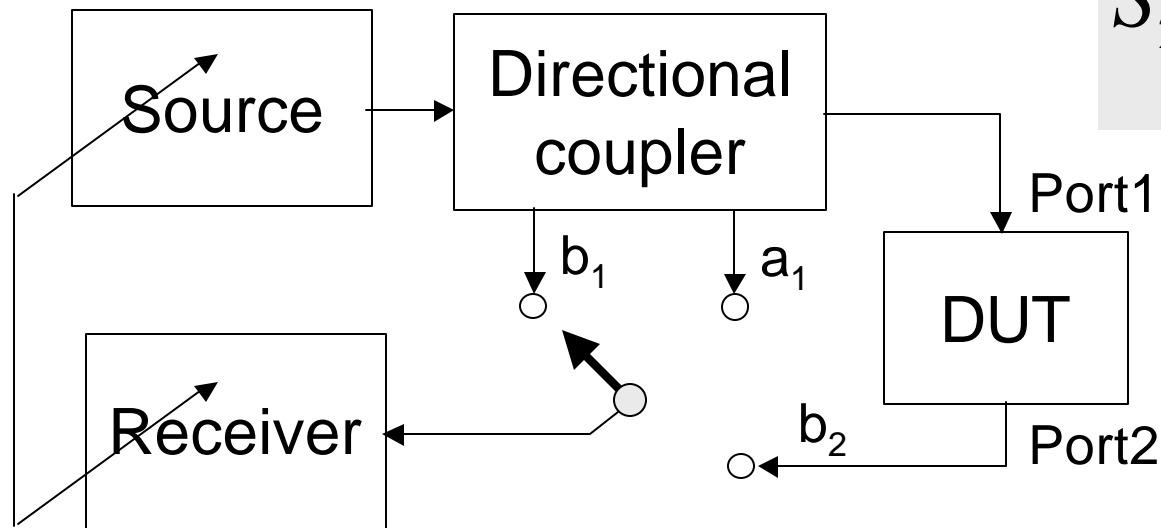
Requirements in Power Distribution



What is a VNA

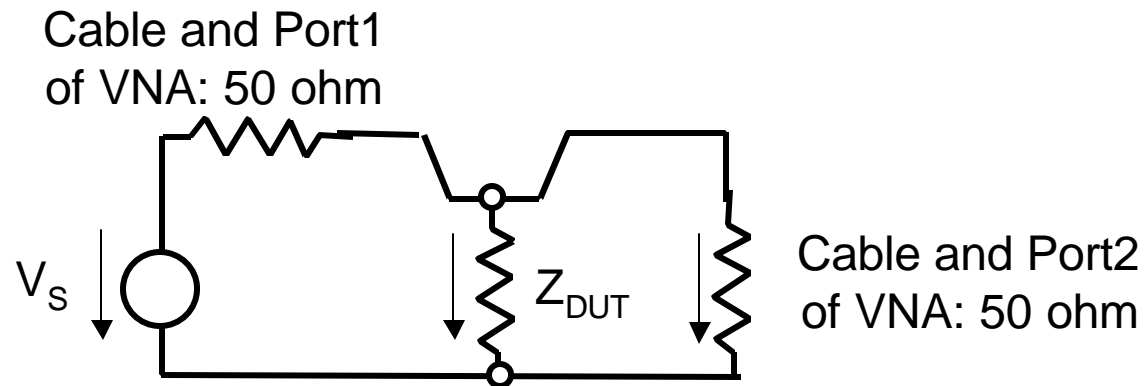
- Tuned sinewave generator
- Directional couplers
- Tracking receiver(s)

$$S_{11} = \frac{b_1}{a_1} \Big|_{a_2=0}$$
$$S_{21} = \frac{b_2}{a_1} \Big|_{a_2=0}$$



Two-Port Self-Impedance Measurement

- S_{21} instead of S_{11} is measured
- S_{21} uncertainty is less
- Z_p is in series to 50 ohms instead of Z_{DUT}



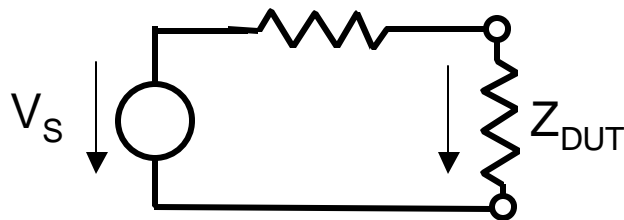
Two-Port Self-Impedance Reading

First-order calculation:

Assume that

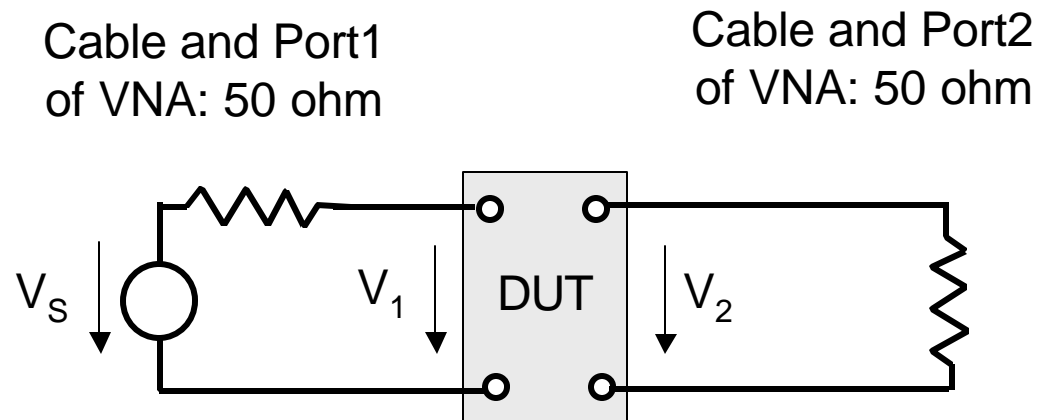
- $L_p \sim 0$
- $Z_{DUT} \ll Z_0$

Port1 and Port 2 of
VNA: 25 ohm



$$Z_{DUT} = Z_{11} = S_{21}^* 25 \text{ [ohm]}$$

Transfer Impedance Measurement



Transfer Impedance Reading

First-order calculation:

Assume that

- $L_p \sim 0$
- $Z_{11} \ll Z_0$
- $Z_{22} \ll Z_0$
- $Z_{21} \ll Z_0$

$$Z_{21} = Z_{12} = S_{21}^* \cdot 25 \text{ [ohm]}$$

S21 Uncertainty

- $|S_{21}|$ uncertainty of HP8720D:

<1dB in the $|S_{21}| > -60$ dB range

<3dB in the $|S_{21}| > -70$ dB range

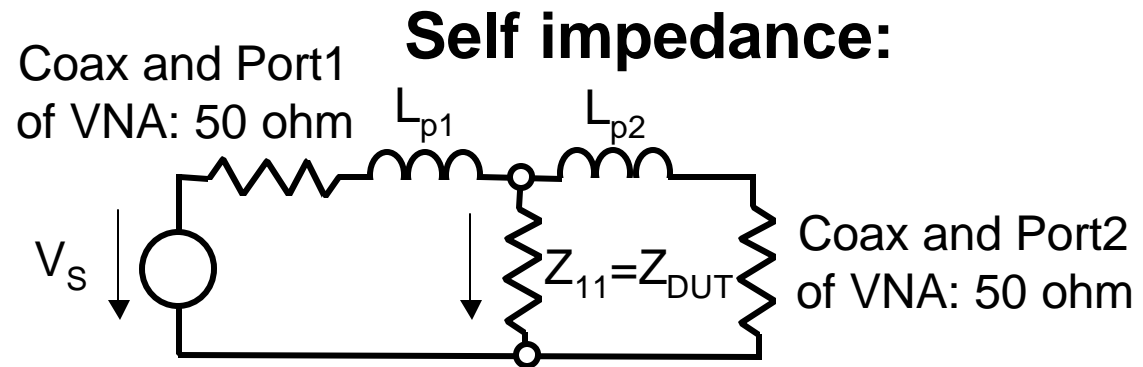
- Impedance uncertainty:

1dB (10%) for $Z_{DUT} >$

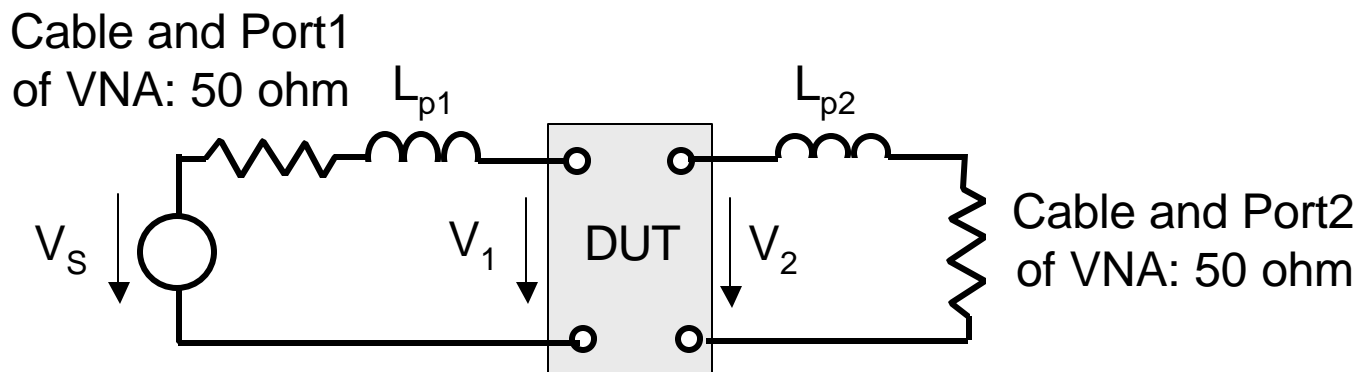
25milliohms

3dB (40%) for $Z_{DUT} > 8$ milliohms

Equivalent Circuit of Probes Connection



Transfer impedance:



S_{21} Conversion to Self Impedance

$$Z_{ii} = S_{21} \frac{Z_1}{2} \frac{1}{1 - S_{21} \frac{Z_1 + Z_2}{2Z_2}} \approx S_{21} * 25 * \frac{1 + j\omega\tau_p}{1 - S_{21}}$$

Where $Z_1 = 50 + j\omega L_{p1}$

$$Z_2 = 50 + j\omega L_{p2}$$

$$\tau_p = L_p / 50$$

S_{21} Conversion to Transfer Impedance

$$Z_{ji} = S_{21} \frac{Z_1}{2} \frac{\left(1 + \frac{Z_{11}}{Z_1}\right) \left(1 + \frac{Z_{22}}{Z_2}\right)}{1 + \frac{S_{21} Z_{21}}{2} \frac{Z_1}{Z_2}} \approx$$

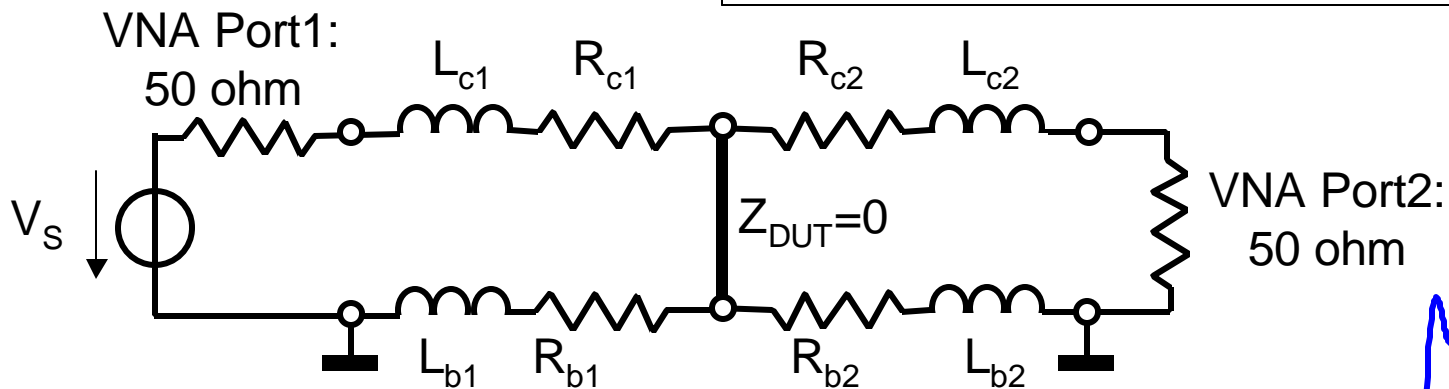
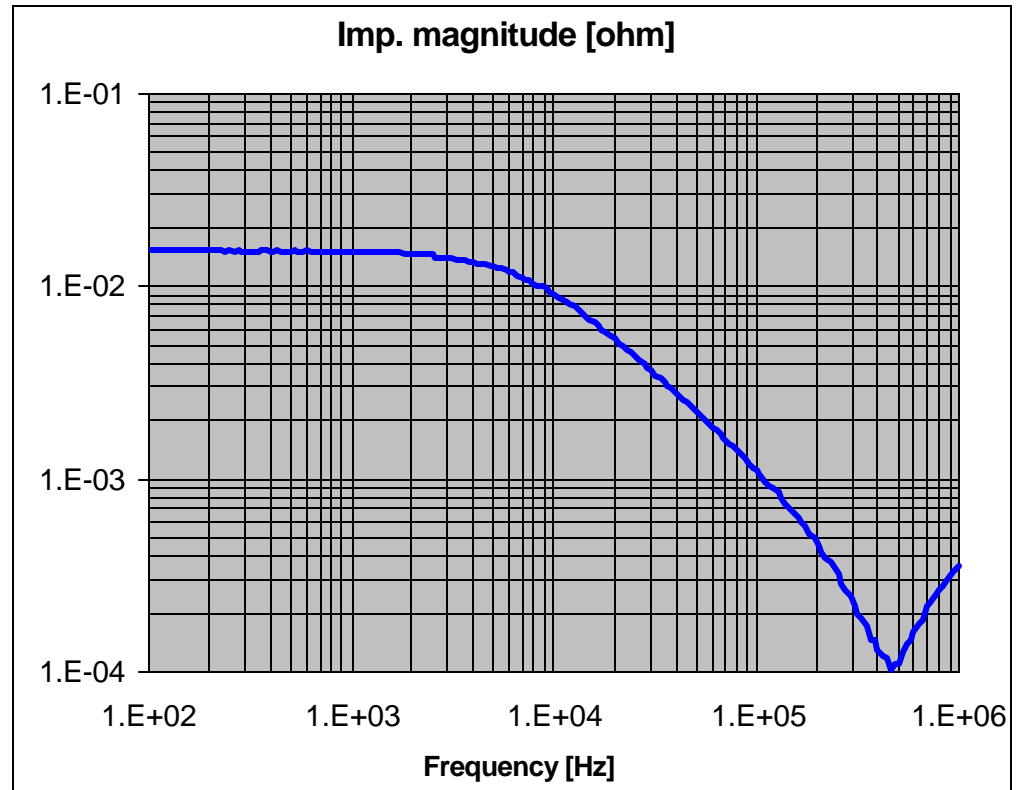
$$S_{21} * 25 * \frac{1 + j\omega\tau_p}{1 + 50 * \left(\frac{S_{21}}{2}\right)^2} * \left(1 + \frac{Z_{11}}{Z_1}\right) \left(1 + \frac{Z_{22}}{Z_2}\right)$$

Where $Z_1 = 50 + j\omega L_{p1}$

$Z_2 = 50 + j\omega L_{p2}$

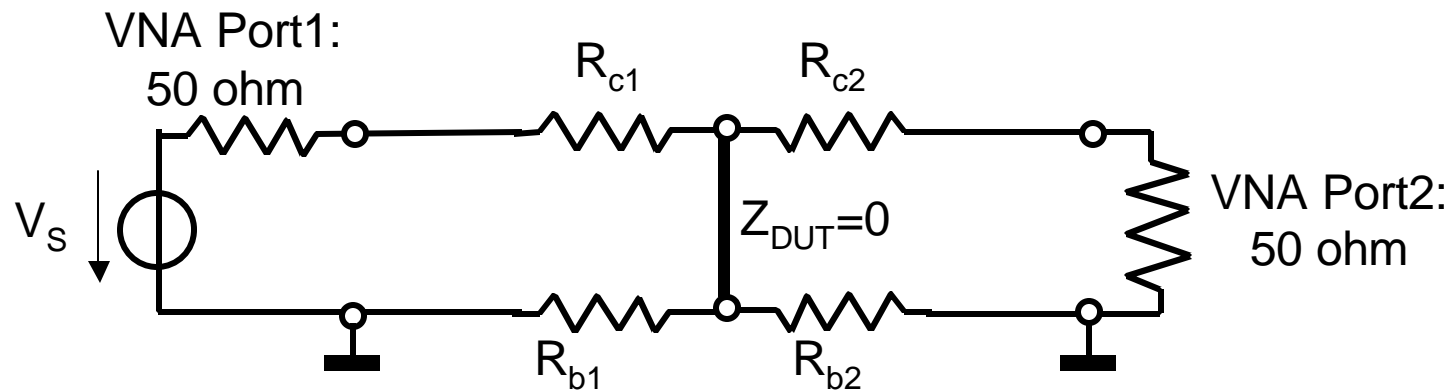
$\tau_p = L_p / 50$

Low-Frequency Ground Loop



Ground-Loop DC Error

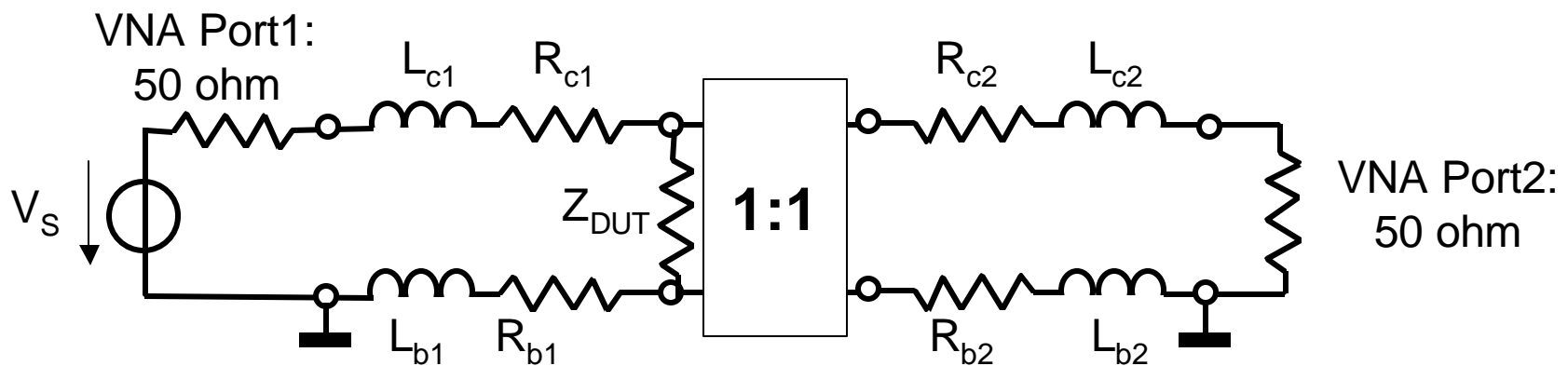
$$R_{DC_error} = R_{b1} \parallel R_{b2}$$



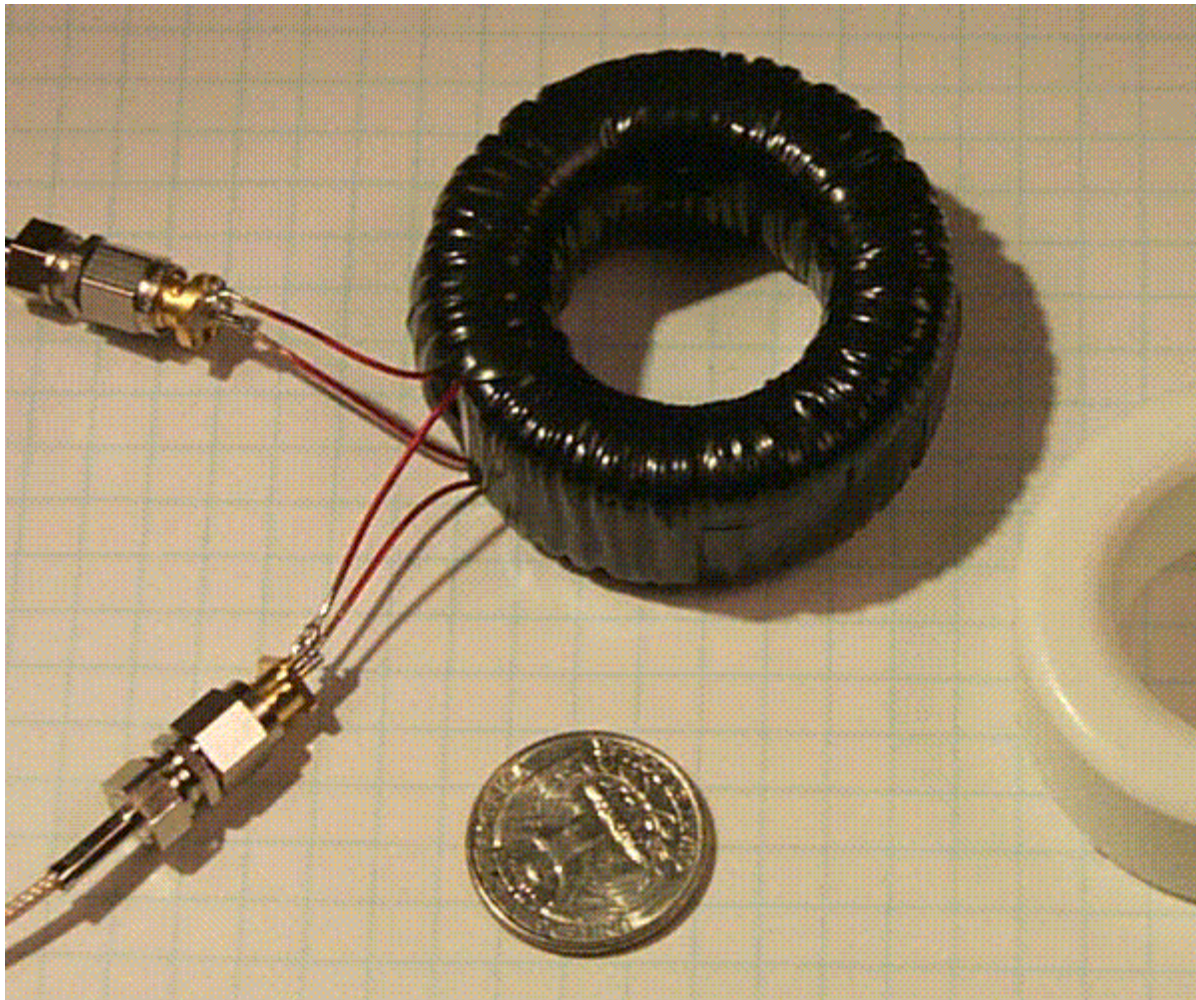
Eliminating Ground Loop

Transformer

Differential amplifier

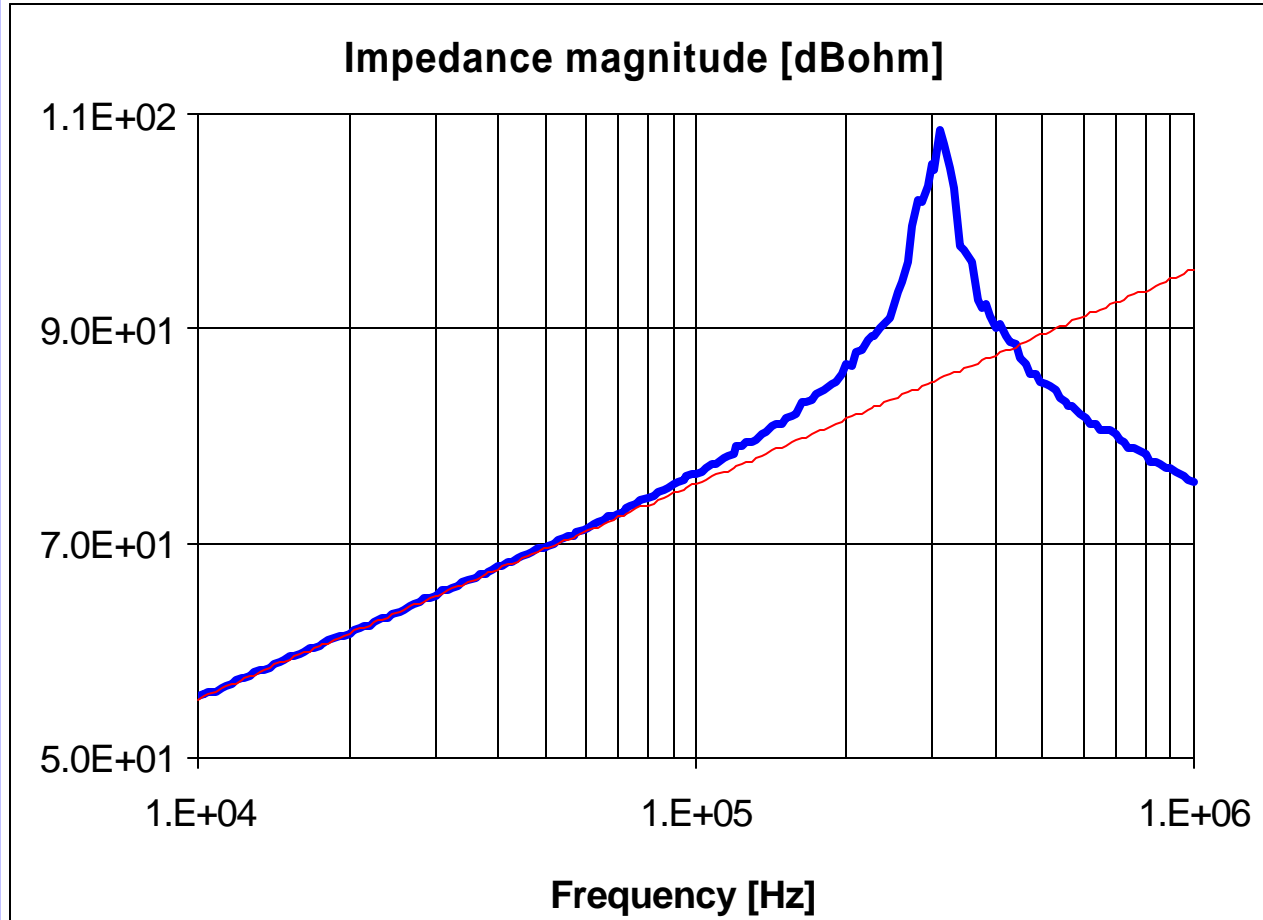


Transformer



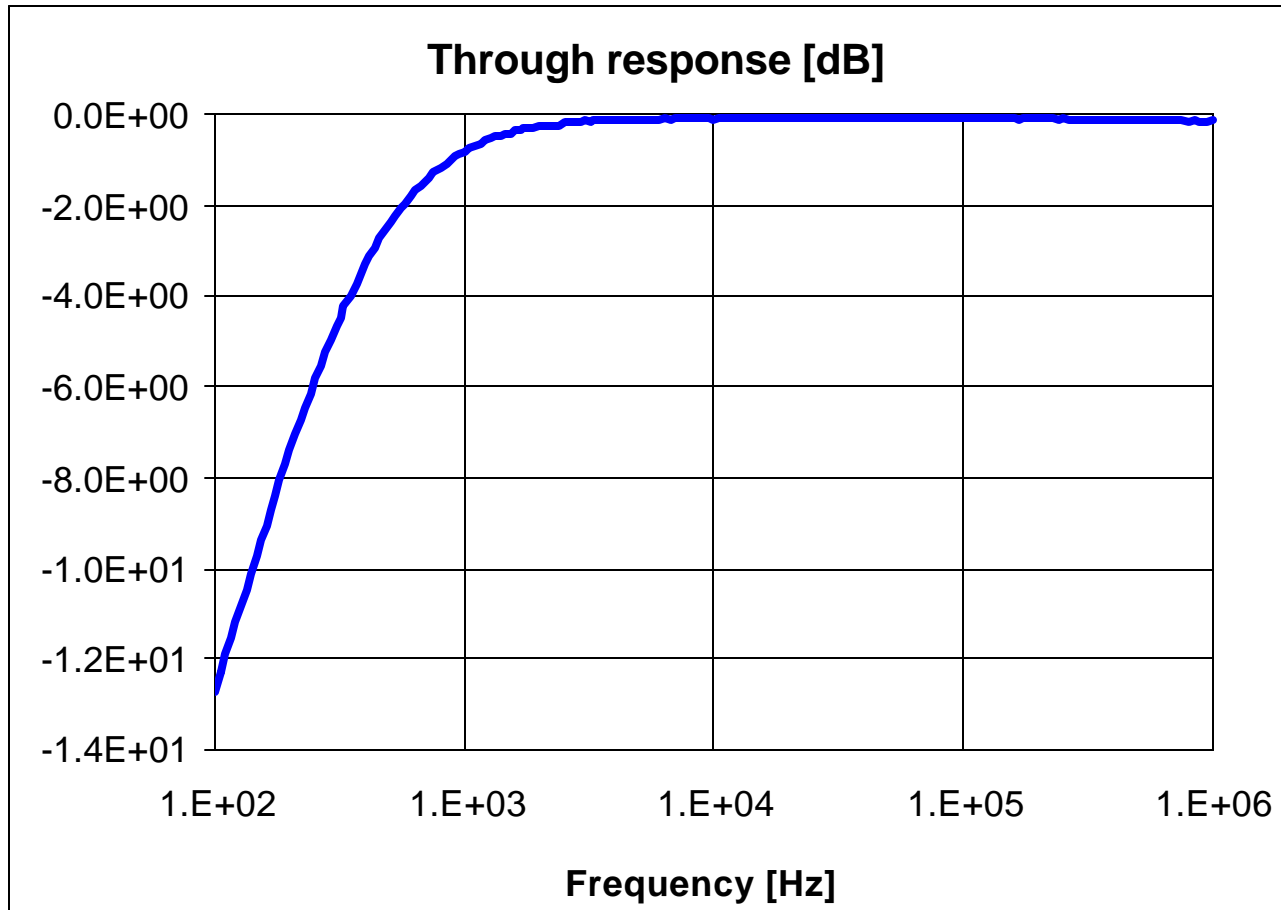
- Phillips core:
TX51/32/19-3F3
- Diameter: 52mm
 - 2x50 turns
 - AWG 20
 - bifilar
 - SMA female

Transformer Impedance



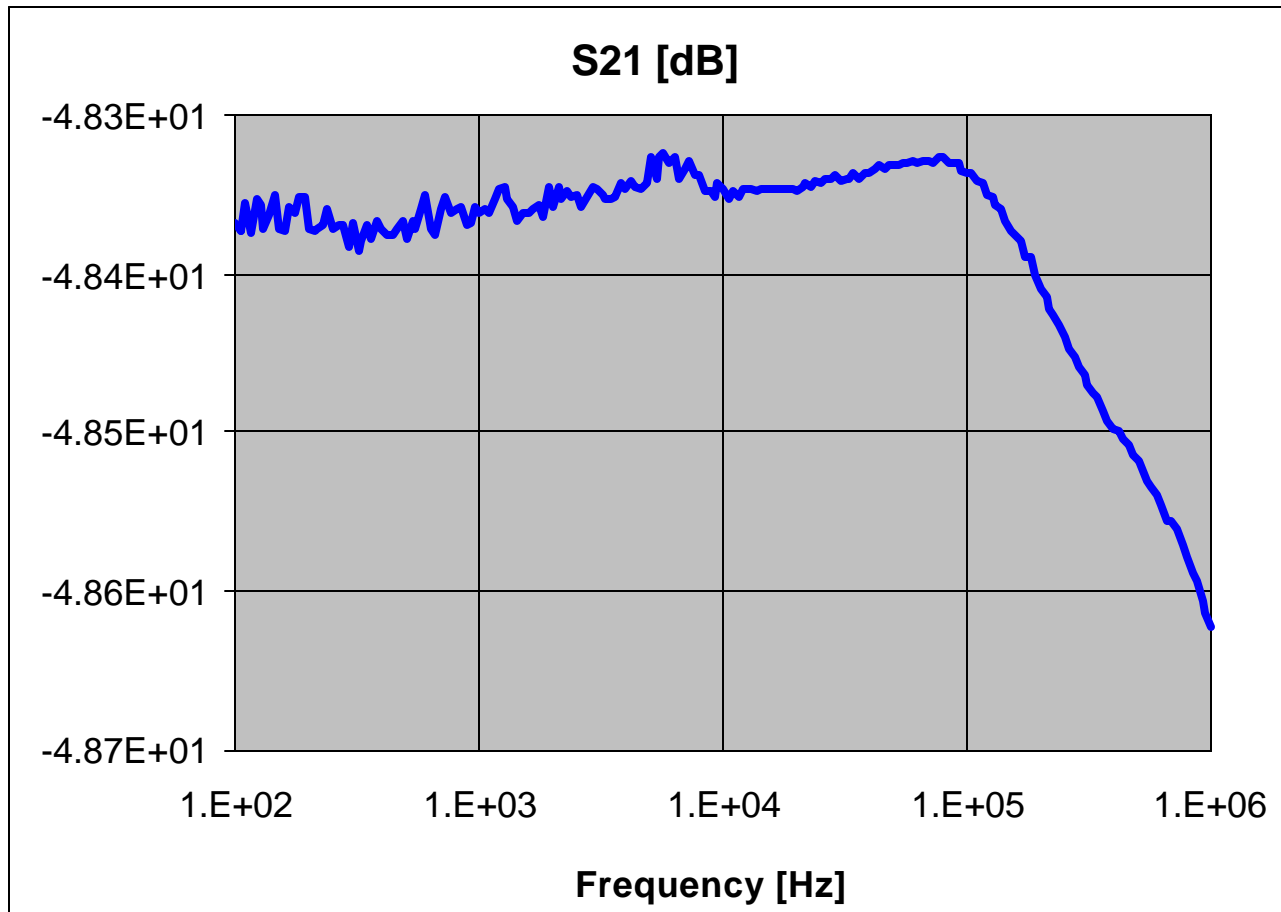
- HP4395B
- HP87512A
- Open secondary
- $L_{\text{main}}=9.5\text{mH}$

Transformer Response (1)



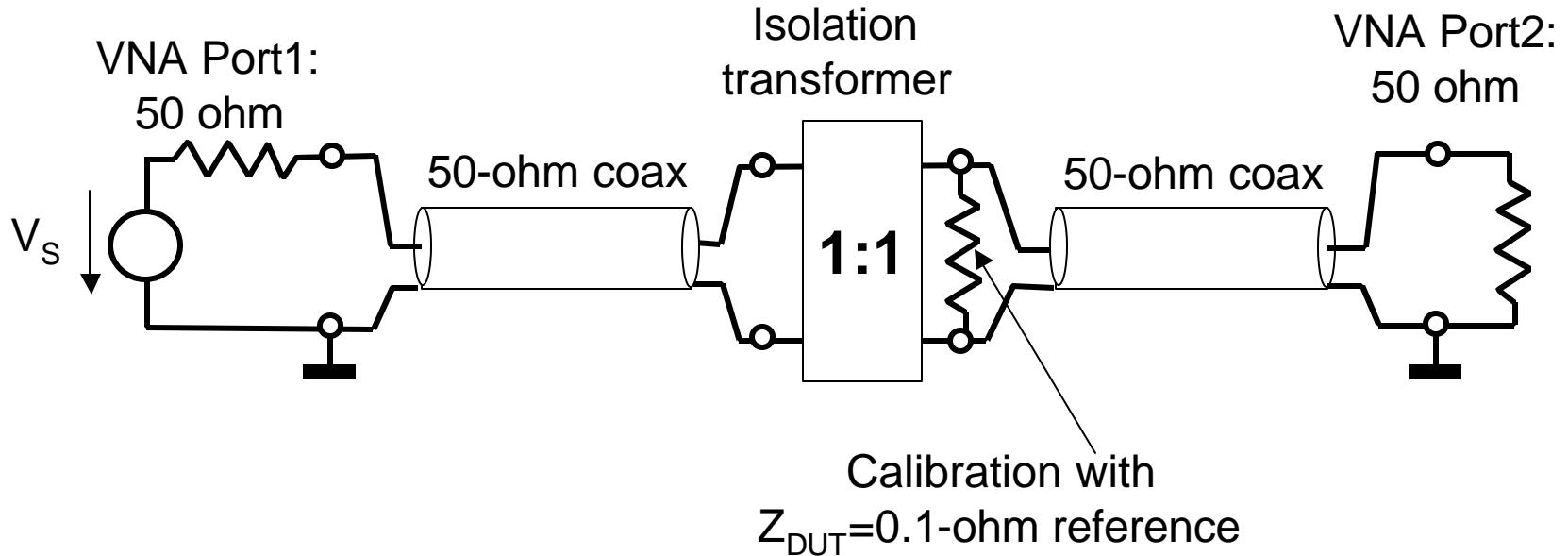
- 1:1 transformer
- HP4395B
- 50 ohms terminations

Transformer Response (2)

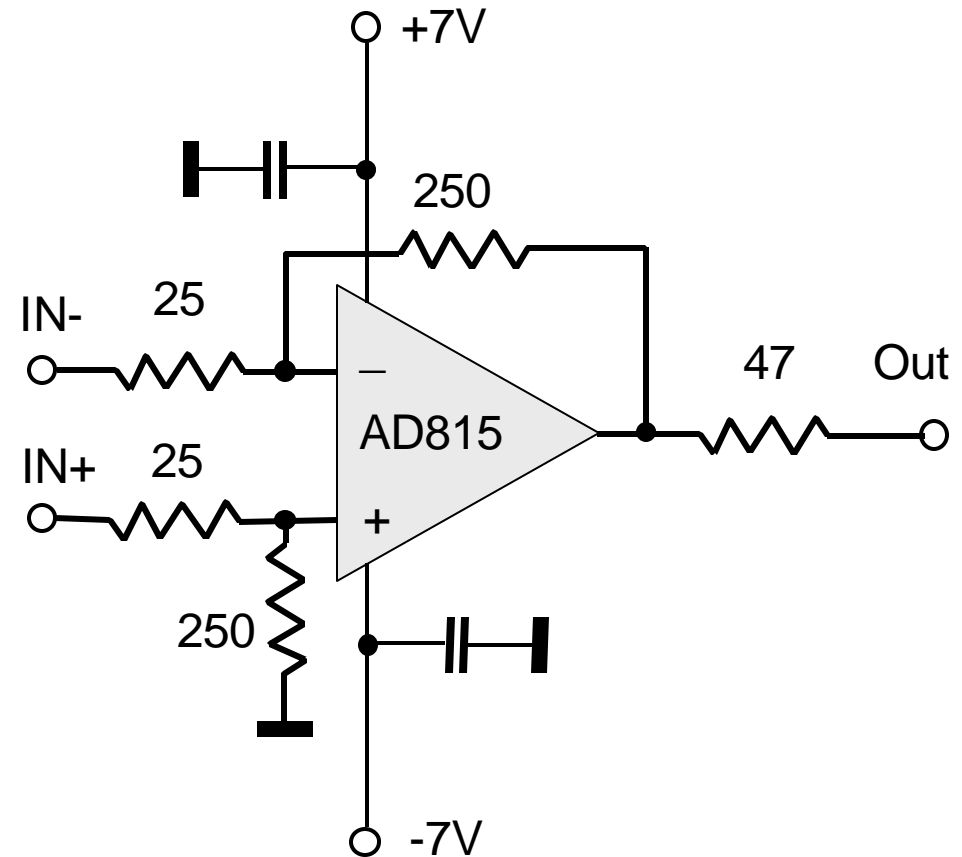
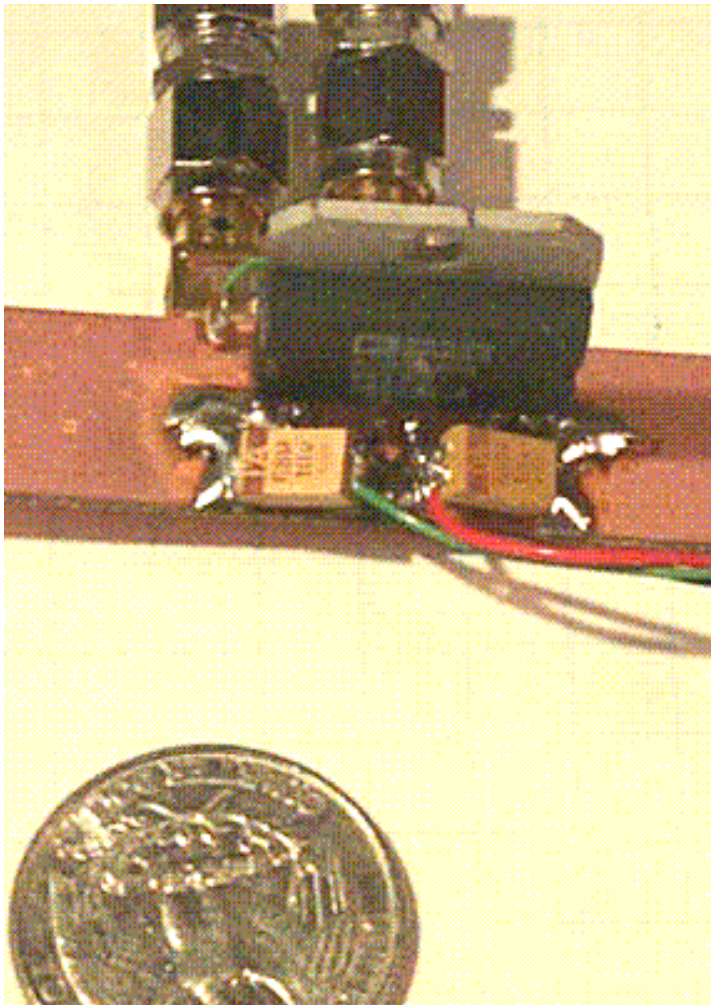


- 1:1 transformer
- HP4395B
- Calibrated with 50 ohms terminations
- 0.1 ohms shunt

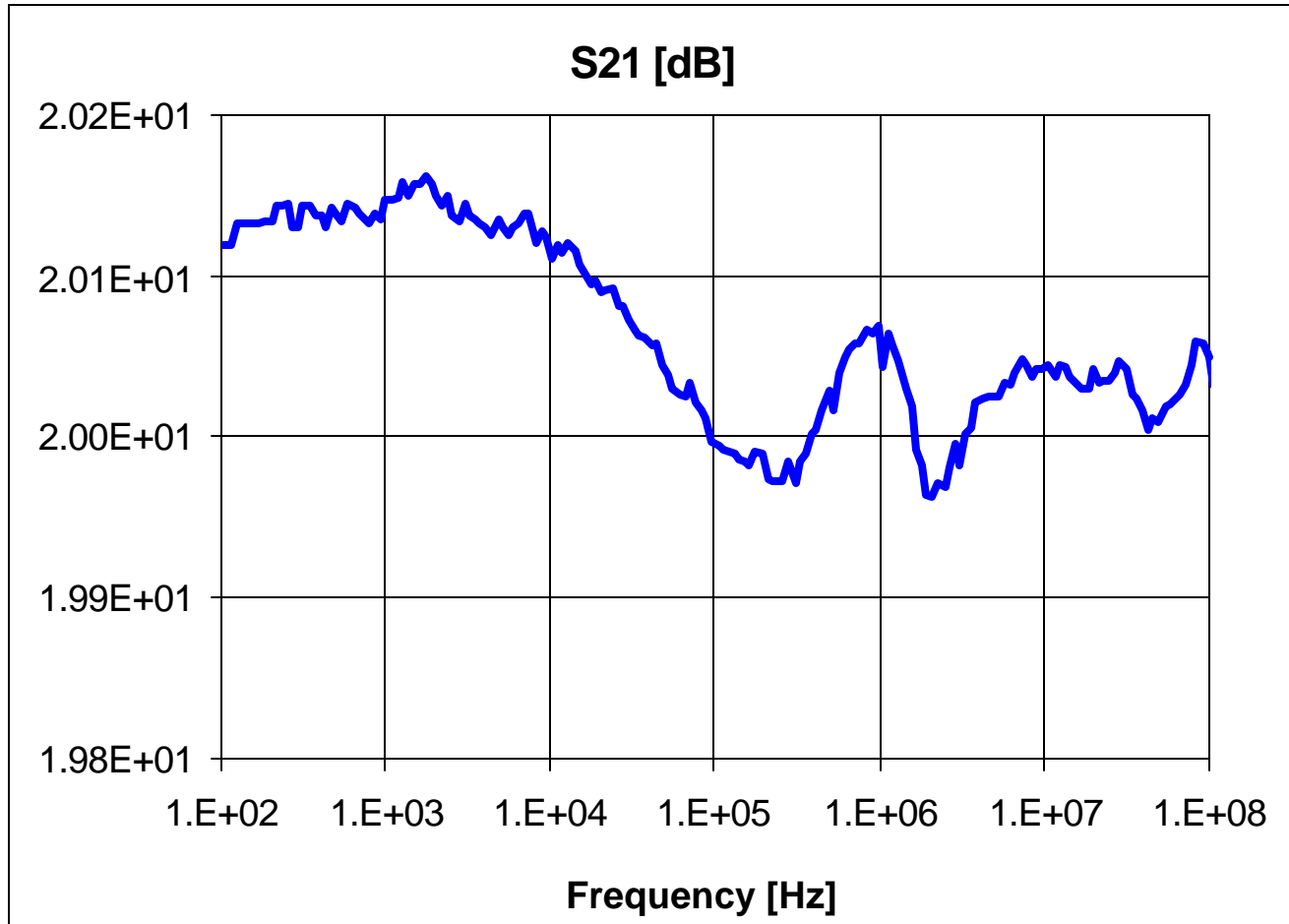
Calibration Setup



Isolation Amplifier

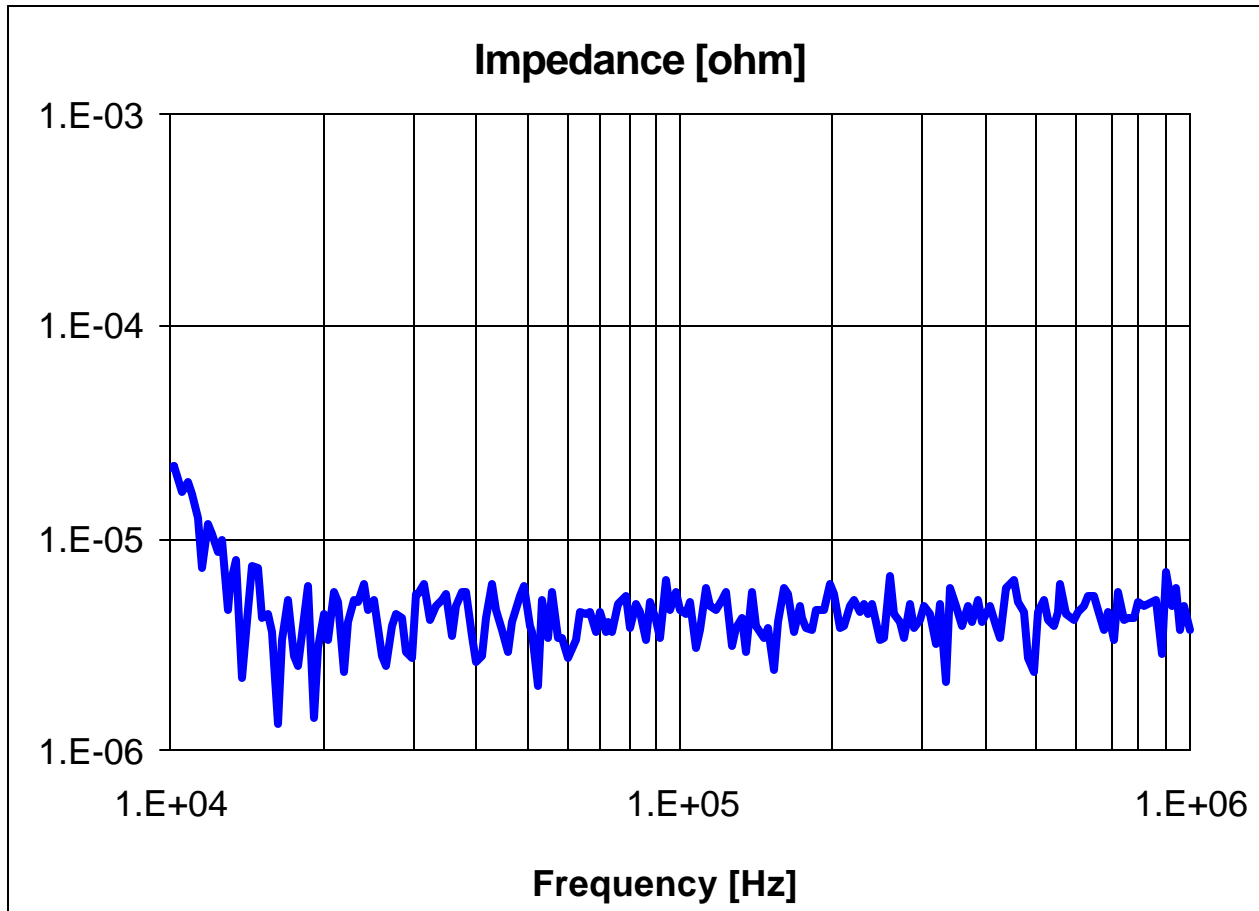


Reduced Error Floor by Increased P

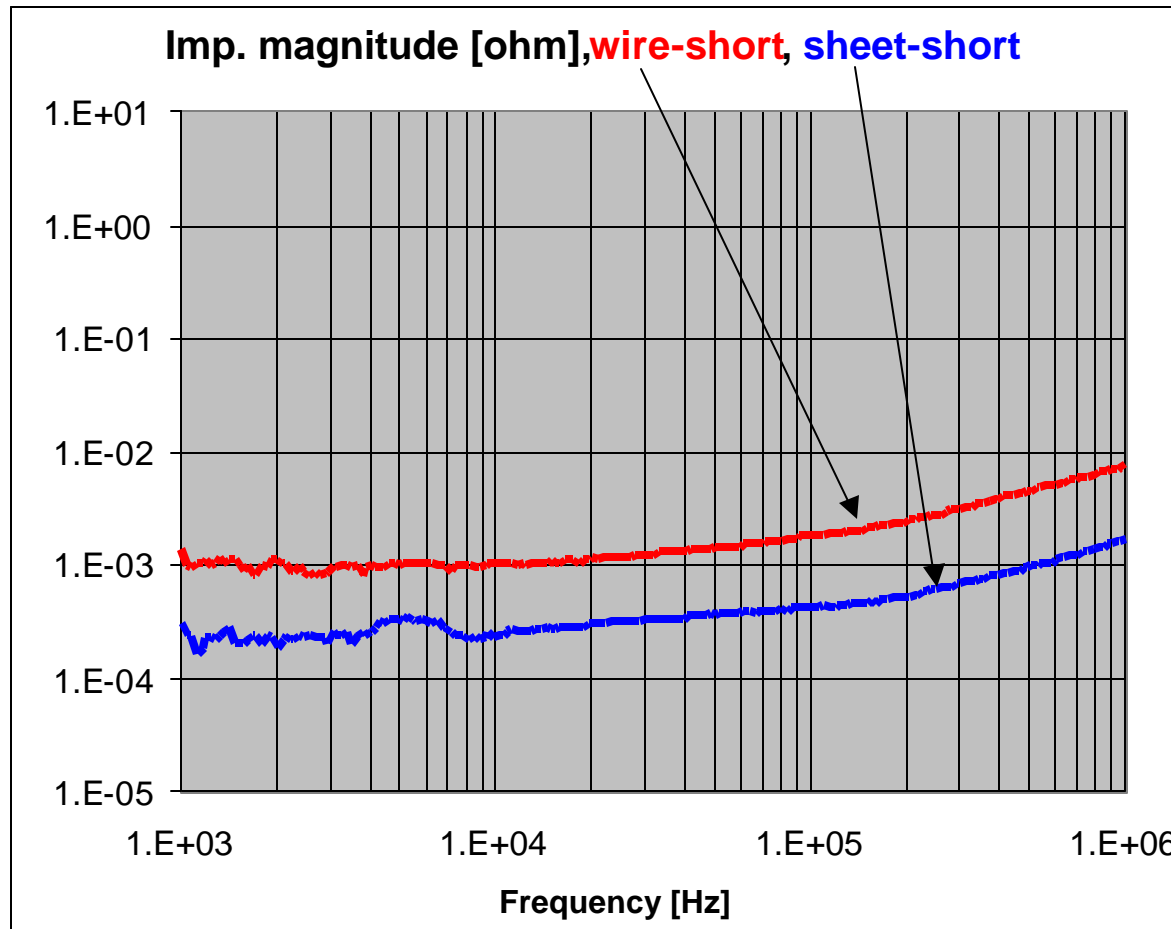


- Calibration at -5dBm
- HP4395B
- Power changed to $+15\text{dBm}$

Residual Noise

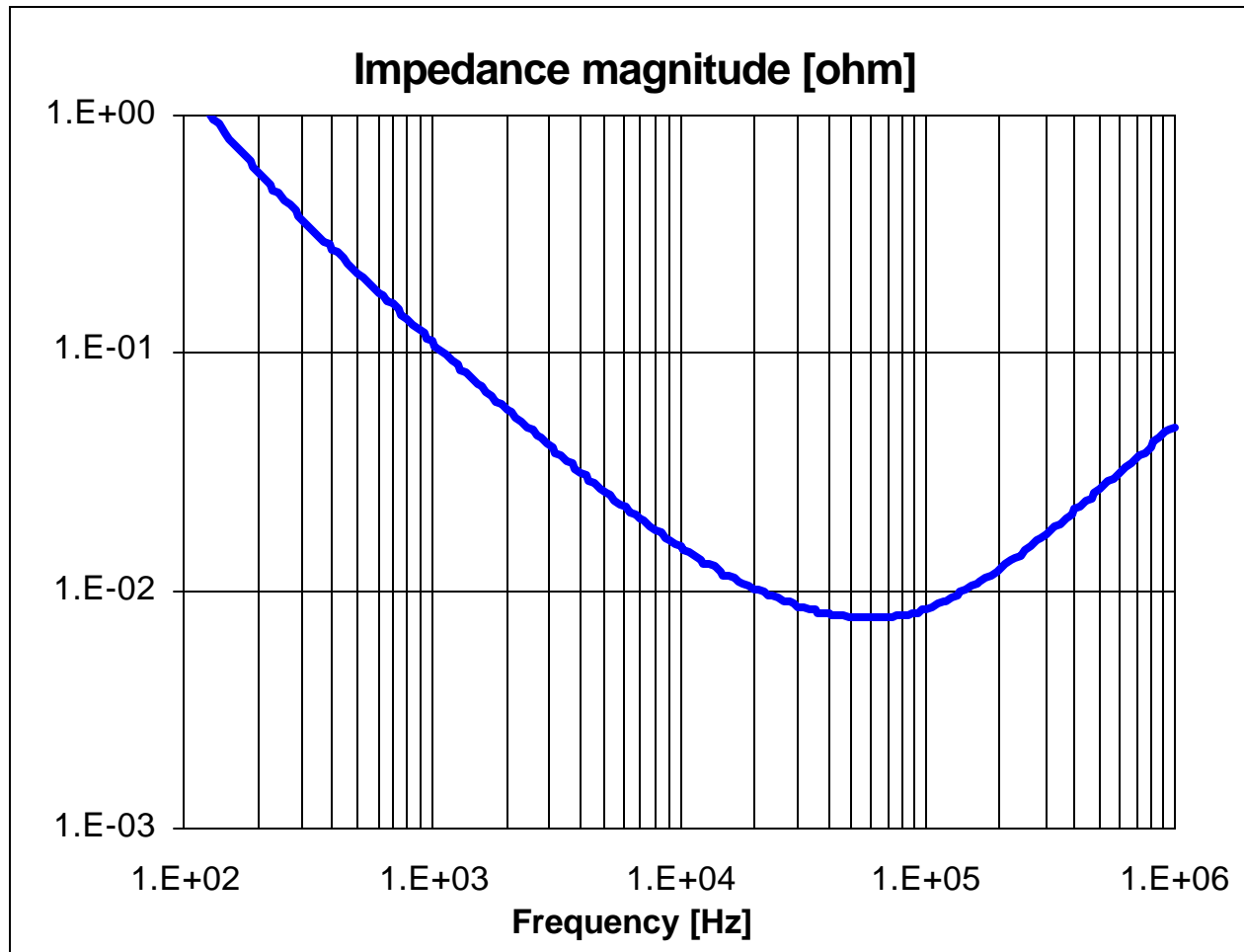


Reading of Shorts



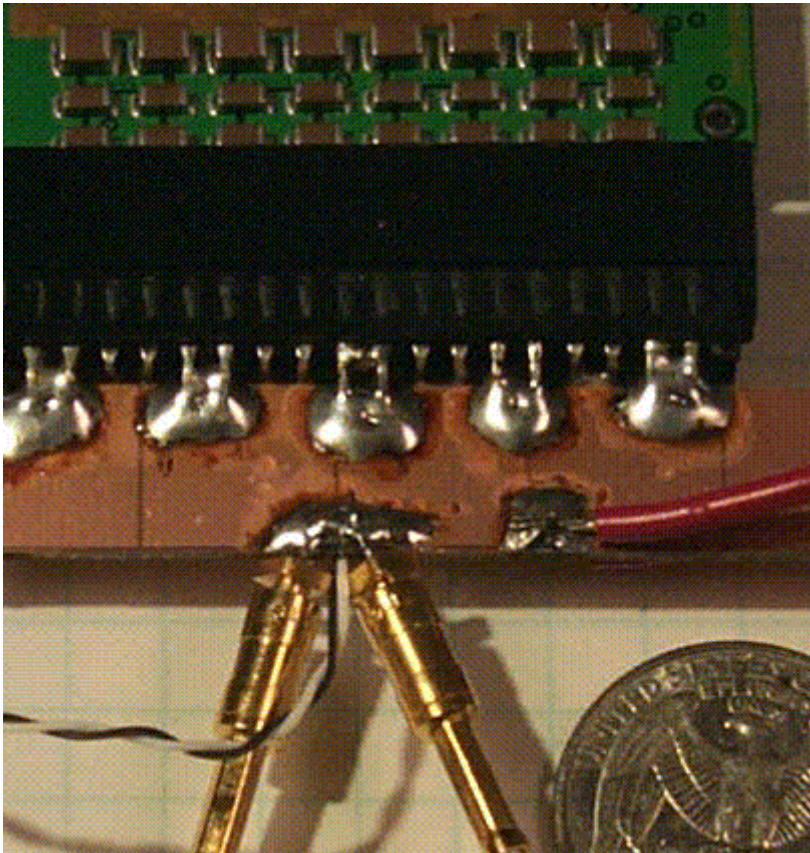
- Isolation transformer
- HP4395B

Measuring Low ESR



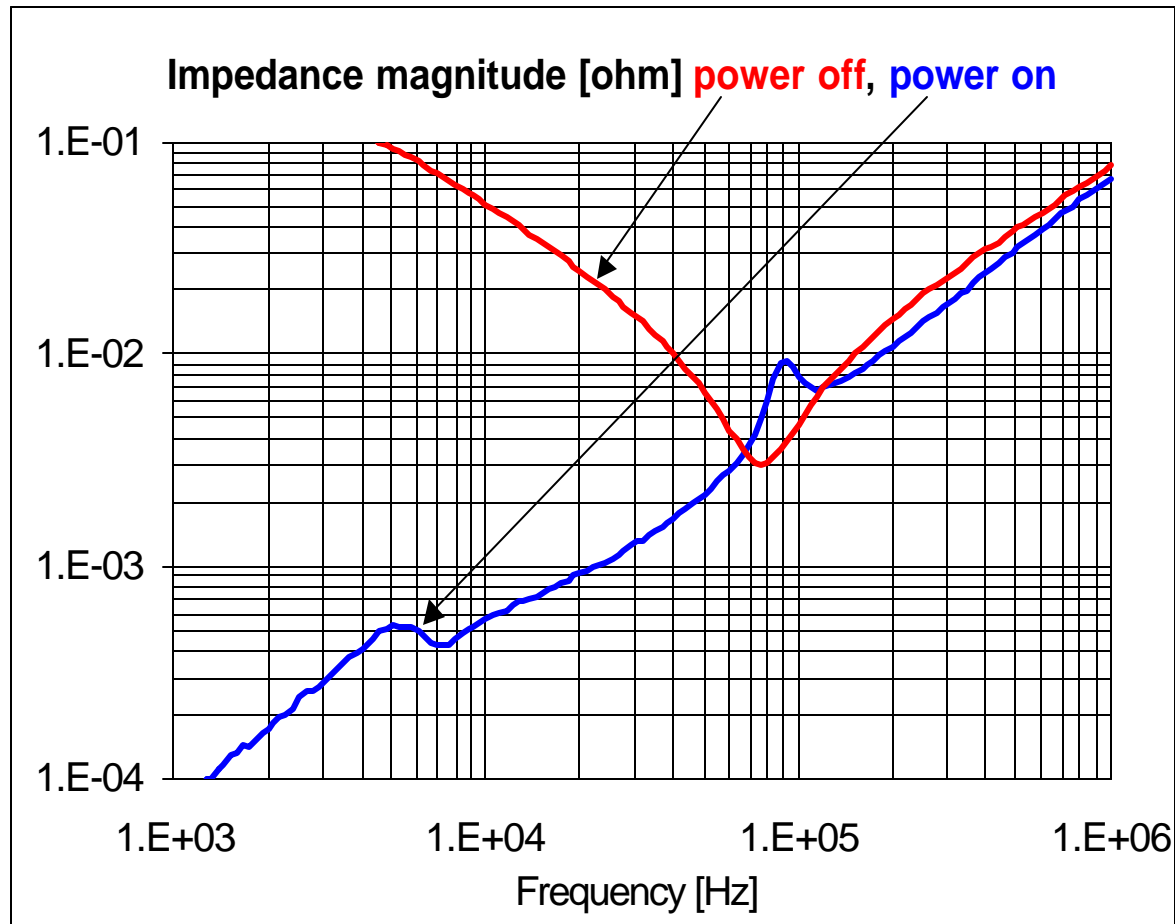
- 1:1 transformer
- HP4395B
- 0.1ohm calibration
- OSCON 1500uF 4V

Voltage Regulator Module



- 1.5V VRM
- Output pins connected by copper planes
- SSMB connectors

VRM Zout



- 1.5V VRM
- No external capacitor

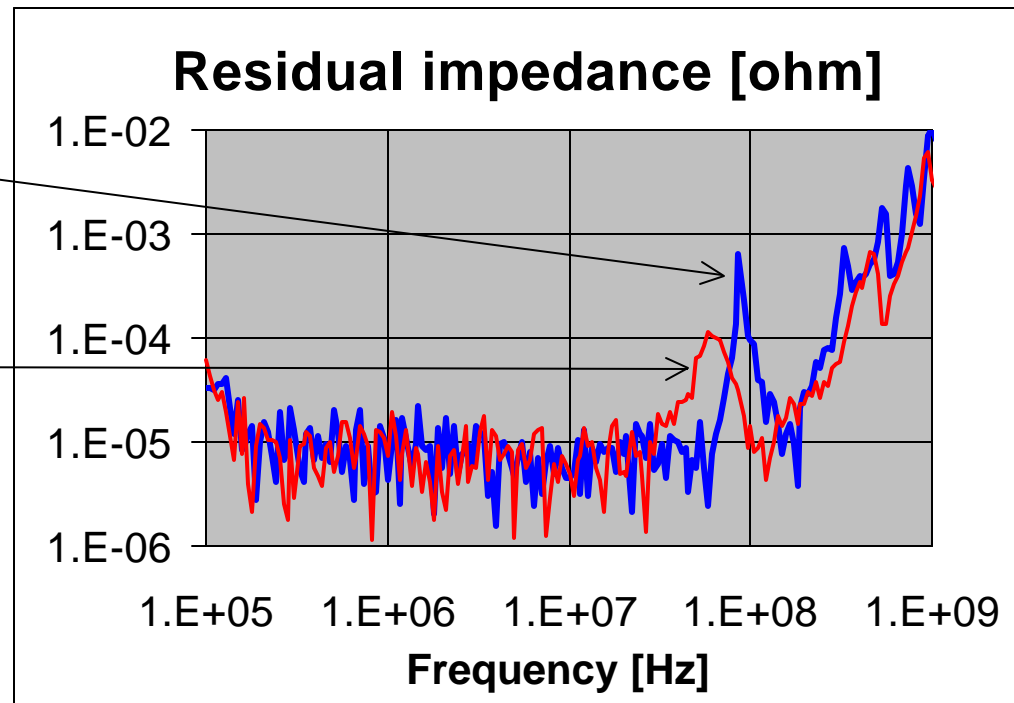
Limitations at High Frequencies

Finite braid surface transfer impedance

Braid resonances

Plain coax

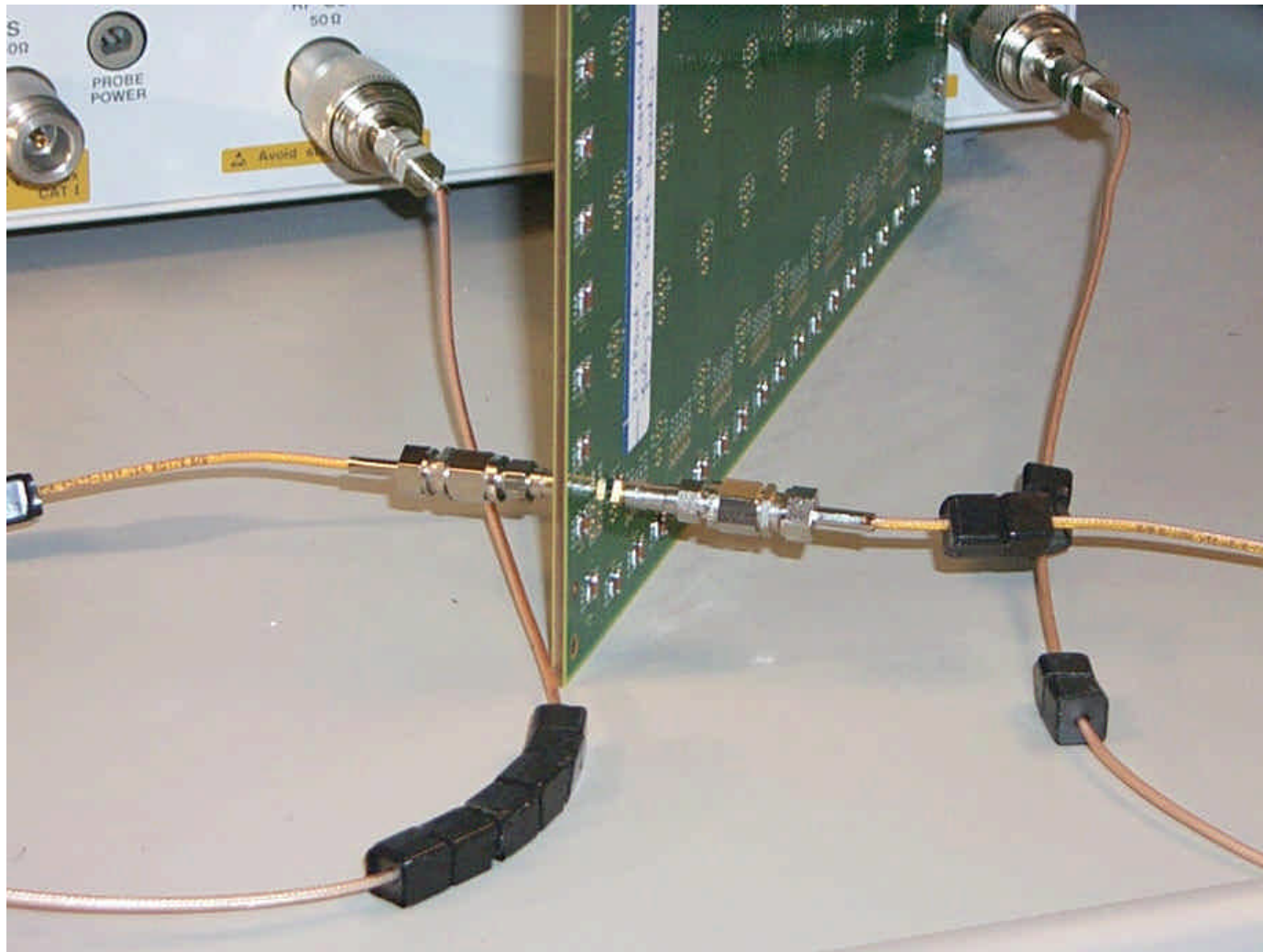
Coax, 2x4 ferrites



Solution:

Absorption ferrites

Ferrite-Covered Cable



Measuring milliohms and picohenrys

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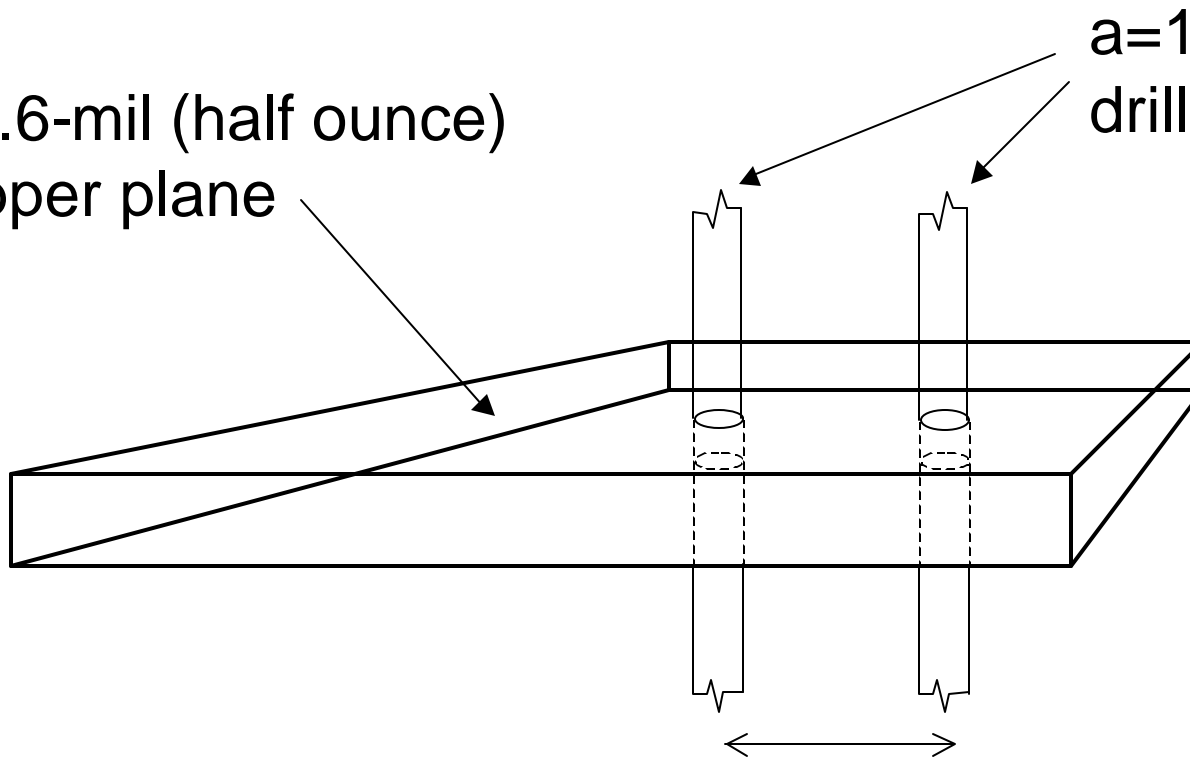
Istvan Novak
DesignCon, Feb. 2000



Reference: Connection to Solid Plane

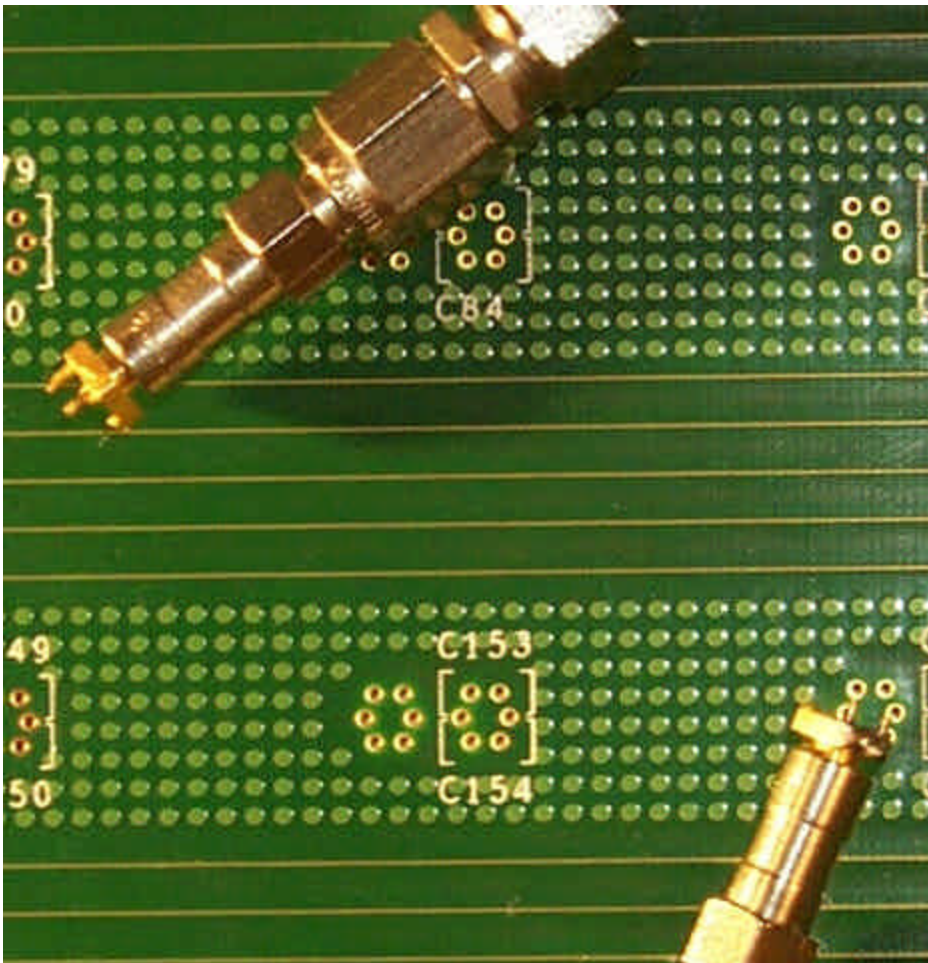
$t=0.6$ -mil (half ounce)
copper plane

$a=15$ -mil radius
drilled vias



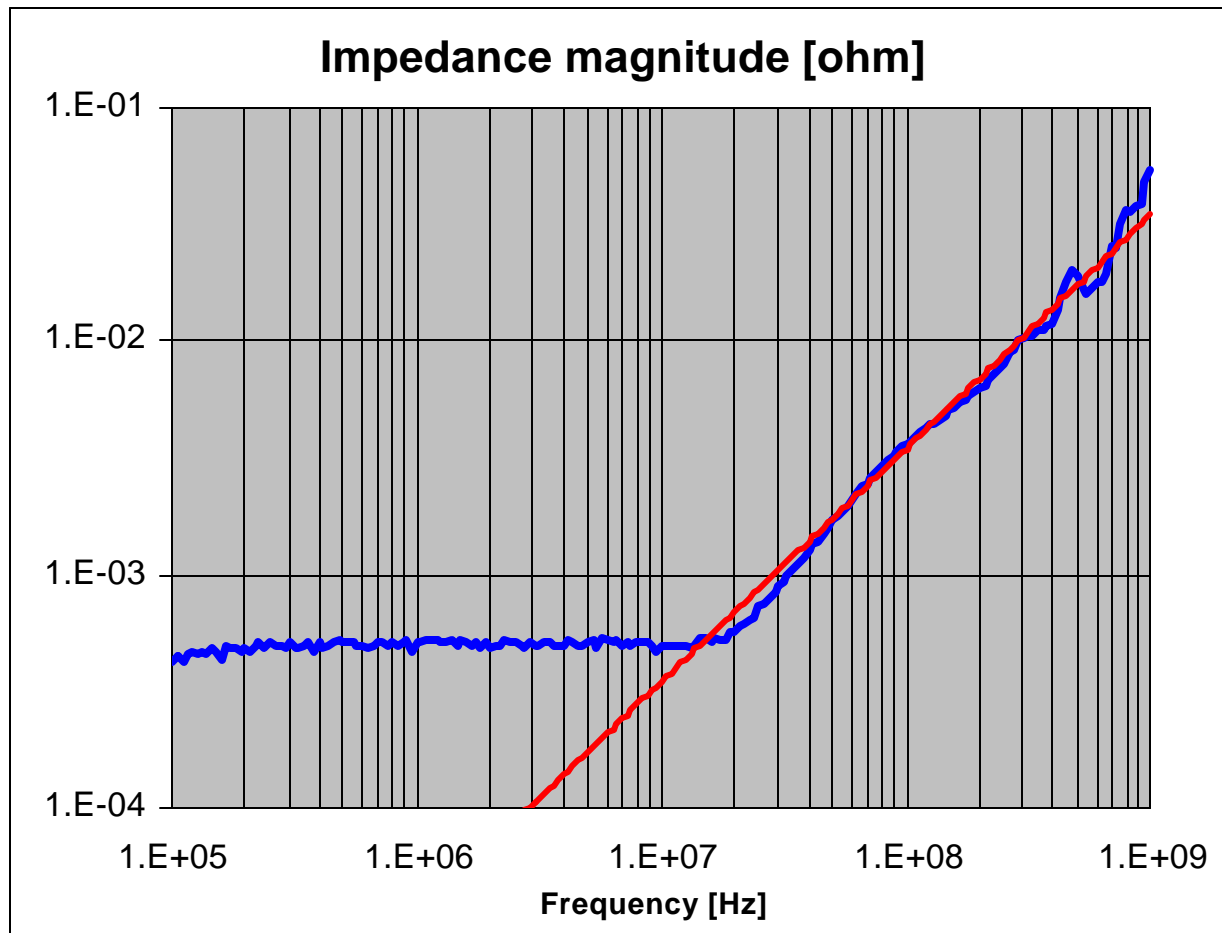
$d=70$ mil center-
to-center spacing

Probes and Vias



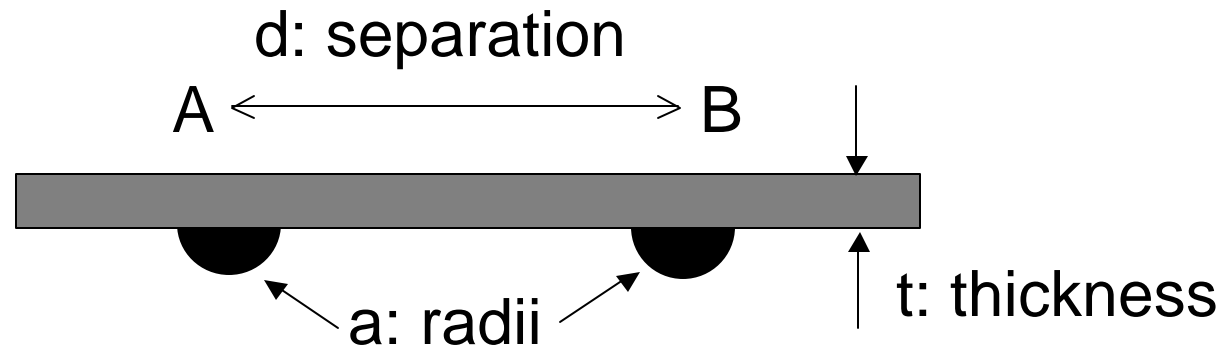
- Test board with via locations
- SMA-SSMB adaptors
- Probe: SSMB jack with two pins

Reading Across Solid Plane



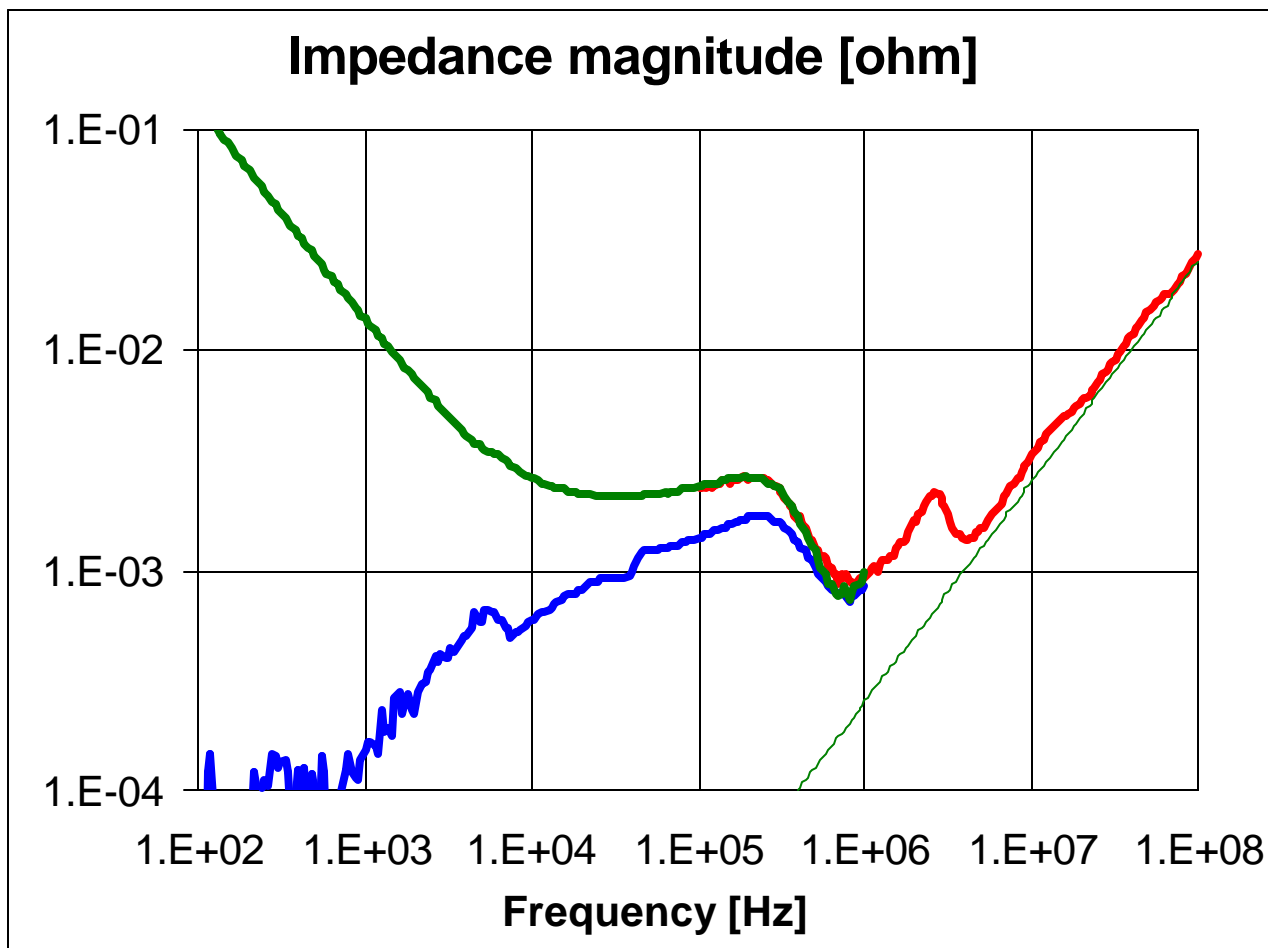
- Half-ounce Cu
- 30-mil vias
- 70-mil via spacing
- 0.52 milliohms
- 5.5pH

DC Resistance Across Solid Plane



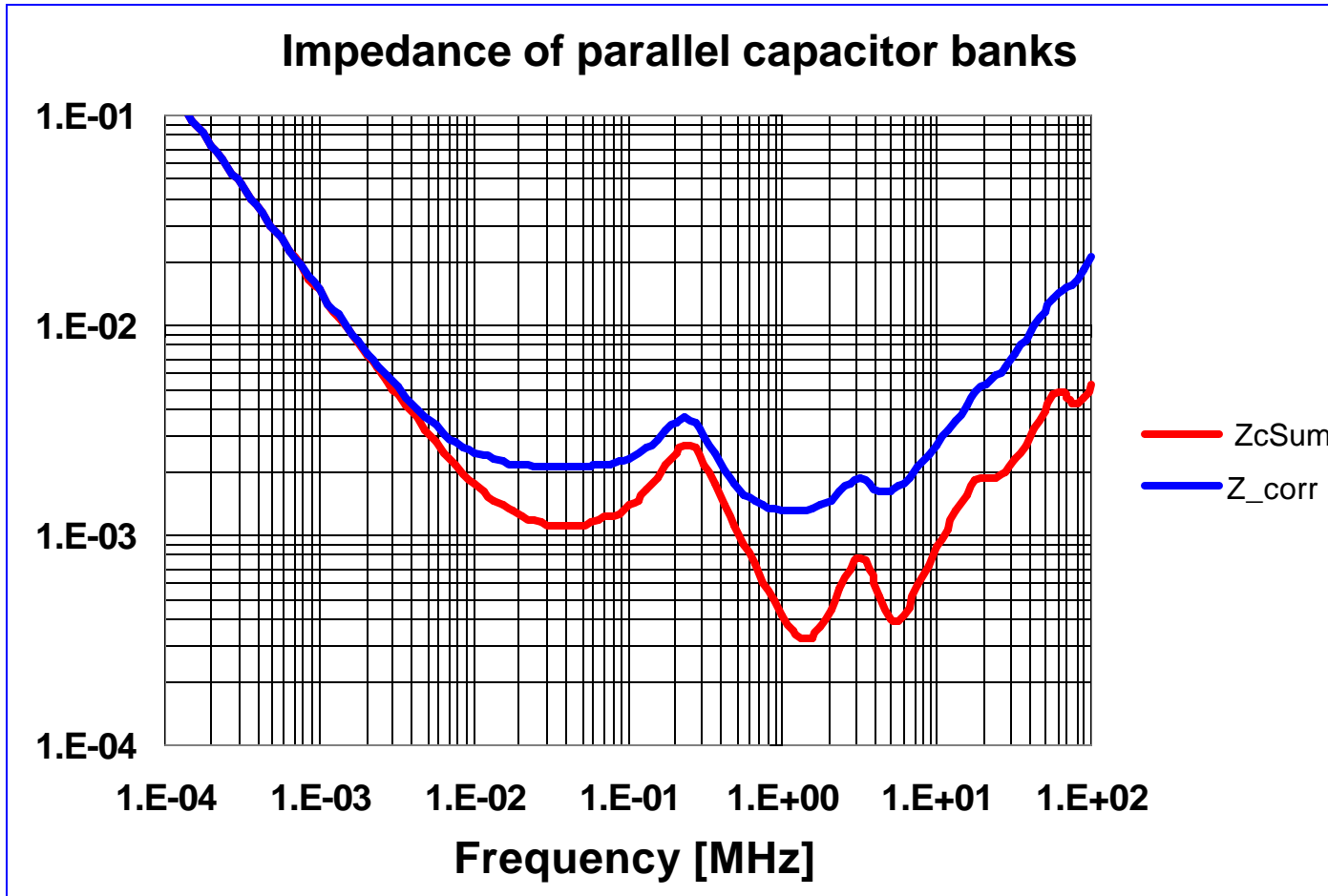
$$R_{AB} \approx \frac{1}{\rho s a} \left[1 + \frac{a}{t} \ln \left(\frac{\sqrt{1 + \left(\frac{d}{2t}\right)^2} + 1}{\sqrt{1 + \left(\frac{a}{2t}\right)^2} + 1} \right) \right]$$

Combined Impedance of PDN



- VRM
- 2x3"x4" 2-mil planes
- Bulk capacitors
- 90 bypass capacitors

Simulated PDN Impedance



Recommended Resources

Hewlett Packard Vector Network Analyzers:

- HP 4395 VNA 10Hz-500MHz
- HP 4396 VNA 100kHz-1.8GHz
- HP87512A DC-2GHz
Transmission/Reflection Test Set
- HP 8720D VNA 50MHz-20GHz

Circuit simulator software:

- Avant! HSPICE

Conclusions

- Two-port measurements reduce effect of discontinuities
- Limitation at low frequencies: cable-braid ground loop
- Ground-loop is eliminated by transformer or amplifier
- Limitation at high frequencies: braid leakage and resonance
- Reliable reading and good correlation to simulations is achieved in the sub-milliohm range